## Maths-it <br> Maths-it Podcast H-05

## Higher GCSE Revision

## Proportionality

## Topics

Solve problems involving direct and inverse proportion, e.g. $y \propto x, y \propto x^{2}, y \propto \frac{1}{x}, y \propto \frac{1}{x^{2}}$ Find and use equations of this type - Relate to the graphs of these equations

## Questions

1. The electric field intensity, $E$, of a charge varies inversely as the square of the distance from it, $d$.

When $d=0.3, E=40$
(a) Find a formula for $E$ in terms of $d$.
(b) Hence, or otherwise, calculate the value of $E$ when $d=2$

$$
E=
$$

2. $\quad p$ is inversely proportional to $\sqrt{ } m$.
$p=22$ when $m=25$
Calculate the value of $p$ when $m=4$
3. 



Graph A


Graph C


Graph B


Graph D

The graphs of $y$ against $x$ represent four different types of proportionality.
Write down the letter of the graph which represents the type of proportionality.

| Type of proportionality | Graph letter |
| :---: | :---: |
| $y$ is directly proportional to $x$ | ...................... |
| $y$ is inversely proportional to $x$ | ..................... |
| $y$ is proportional to the square of $x$ | ...................... |
| $y$ is inversely proportional to the square of $x$ | ...................... |

4. The kinetic energy, $K$ Joules, of a moving object is directly proportional to the square of its velocity, $v \mathrm{~m} / \mathrm{s}$.

When $v=6 \mathrm{~m} / \mathrm{s}, K=90 \mathrm{~J}$
Find the value of $v$ when $K=40$

$$
v=.
$$

$\qquad$
(Total 4 marks)
5. $\quad p$ is inversely proportional to $q$.
$p=15$ when $q=0.15$
Calculate the value of $p$ when $q=6$.
(Total 3 marks)
6. The weight of a length of climbing rope is directly proportional to its length.

A 40 m length of rope has a weight of 2.4 kilograms.
Another length of the same rope is 55 m long.
Calculate the weight of the 55 m length of rope.

## Proportionality

7. 

Graph A


Graph C


Graph B


Graph D


For $k>0$ each graph matches with one of the equations,

$$
y=k x \quad y=k \sqrt{x} \quad y=\frac{k}{x} \quad y=k x^{2}
$$

Match each graph to its equation,

| Equation | Graph |
| :--- | :--- |
| $y=k x$ |  |
| $y=k \sqrt{x}$ |  |
| $y=\frac{k}{x}$ |  |
| $y=k x^{2}$ |  |

